6. Is it possible to convert internal energy to mechanical energy? Explain with examples.
7. It is the morning of a day that will become hot. You just purchased drinks for a picnic and are loading them, with ice, into a chest in the back of your car. (a) You wrap a wool blanket around the chest. Does doing so help to keep the beverages cool, or should you expect the wool blanket to warm them up? Explain your answer. (b) Your younger sister suggests you wrap her up in another wool blanket to keep her cool on the hot day like the ice chest. Explain your response to her.
8. You need to pick up a very hot cooking pot in your kitchen. You have a pair of cotton oven mitts. To pick up the pot most comfortably, should you soak them in cold water or keep them dry?
9. Suppose you pour hot coffee for your guests, and one of them wants it with cream. He wants the coffee to be as warm as possible several minutes later when he drinks it. To have the warmest coffee, should the person add the cream just after the coffee is poured or just before drinking? Explain.
10. When camping in a canyon on a still night, a camper notices that as soon as the sun strikes the surrounding peaks, a breeze begins to stir. What causes the breeze?
11. Rub the palm of your hand on a metal surface for about 30 seconds. Place the palm of your other hand on an unrubbed portion of the surface and then on the rubbed portion. The rubbed portion will feel warmer. Now repeat this process on a wood surface. Why does the temperature difference between the rubbed and unrubbed portions of the wood surface seem larger than for the metal surface?
12. In 1801, Humphry Davy rubbed together pieces of ice inside an icehouse. He made sure that nothing in the environment was at a higher temperature than the rubbed pieces. He observed the production of drops of liquid water. Make a table listing this and other experiments or processes to illustrate each of the following situations. (a) A system can absorb energy by heat, increase in internal energy, and increase in temperature. (b) A system can absorb energy by heat and increase in internal energy without an increase in temperature. (c) A system can absorb energy by heat without increasing in temperature or in internal energy. (d) A system can increase in internal energy and in temperature without absorbing energy by heat. (e) A system can increase in internal energy without absorbing energy by heat or increasing in temperature.

## Problems

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WebAssign The problems found in this chapter may be assigned online in Enhanced WebAssign
1. denotes straightforward problem; 2. denotes intermediate problem; 3. denotes challenging problem
1. full solution available in the Student Solutions Manual/Study Guide
1. denotes problems most often assigned in Enhanced WebAssign; these provide students with targeted feedback and either a Master It tutorial or a Watch It solution video.
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denotes asking for quantitative and conceptual reasoningdenotes symbolic reasoning problem

M denotes Master It tutorial available in Enhanced WebAssign
GP denotes guided problem
shaded denotes "paired problems" that develop reasoning with symbols and numerical values
3. A combination of 0.250 kg of water at $20.0^{\circ} \mathrm{C}, 0.400 \mathrm{~kg}$ of aluminum at $26.0^{\circ} \mathrm{C}$, and 0.100 kg of copper at $100^{\circ} \mathrm{C}$ is mixed in an insulated container and allowed to come to thermal equilibrium. Ignore any energy transfer to or from the container. What is the final temperature of the mixture?
4. Consider Joule's apparatus described in Figure 20.1. The mass of each of the two blocks is 1.50 kg , and the insulated tank is filled with 200 g of water. What is the increase in the water's temperature after the blocks fall through a distance of 3.00 m ?
5. What mass of water at $25.0^{\circ} \mathrm{C}$ must be allowed to come to thermal equilibrium with a $1.85-\mathrm{kg}$ cube of aluminum initially at $150^{\circ} \mathrm{C}$ to lower the temperature of the aluminum to $65.0^{\circ} \mathrm{C}$ ? Assume any water turned to steam subsequently condenses.
6. The temperature of a silver bar rises by $10.0^{\circ} \mathrm{C}$ when it absorbs 1.23 kJ of energy by heat. The mass of the bar is 525 g . Determine the specific heat of silver from these data.
7. In cold climates, including the northern United States, a house can be built with very large windows facing south to take advantage of solar heating. Sunlight shining in during the daytime is absorbed by the floor, interior walls, and objects in the room, raising their temperature to $38.0^{\circ} \mathrm{C}$. If the house is well insulated, you may model it as losing energy by heat steadily at the rate 6000 W on a day in April when the average exterior temperature is $4^{\circ} \mathrm{C}$ and when the conventional heating system is not used at all. During the period between 5:00 p.m. and 7:00 a.m., the temperature of the house drops and a sufficiently large "thermal mass" is required to keep it from dropping too far. The thermal mass can be a large quantity of stone (with specific heat $850 \mathrm{~J} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}$ ) in the floor and the interior walls exposed to sunlight. What mass of stone is required if the temperature is not to drop below $18.0^{\circ} \mathrm{C}$ overnight?
8. An aluminum cup of mass 200 g contains 800 g of water in thermal equilibrium at $80.0^{\circ} \mathrm{C}$. The combination of cup and water is cooled uniformly so that the temperature decreases by $1.50^{\circ} \mathrm{C}$ per minute. At what rate is energy being removed by heat? Express your answer in watts.
9. A $1.50-\mathrm{kg}$ iron horseshoe initially at $600^{\circ} \mathrm{C}$ is dropped into a bucket containing 20.0 kg of water at $25.0^{\circ} \mathrm{C}$. What is the final temperature of the water-horseshoe system? Ignore the heat capacity of the container and assume a negligible amount of water boils away.
10. Q|C An electric drill with a steel drill bit of mass $m=$ 27.0 g and diameter 0.635 cm is used to drill into a cubical steel block of mass $M=240 \mathrm{~g}$. Assume steel has the same properties as iron. The cutting process can be modeled as happening at one point on the circumference of the bit. This point moves in a helix at constant tangential speed $40.0 \mathrm{~m} / \mathrm{s}$ and exerts a force of constant magnitude 3.20 N on the block. As shown in Figure P20.10, a groove in the bit carries the chips up to the top of the block, where they form a pile around the hole. The drill is turned on and drills into the block for a time interval of 15.0 s. Let's assume this time interval is long enough for conduction within the steel to bring it all to a uniform temperature. Furthermore, assume the steel objects lose a negligible amount of energy by conduction, convection, and radiation into their environment. (a) Suppose the drill bit cuts three-quarters of the way through the block during 15.0 s . Find the temperature change of the whole quantity of steel. (b) What If? Now suppose the drill bit is dull and cuts only
one-eighth of the way through the block in 15.0 s . Identify the temperature change of the whole quantity of steel in this case. (c) What pieces of data, if any, are unnecessary for the solution? Explain.
11. Q|C An aluminum calorimeter with a mass of 100 g contains 250 g of water. The calorimeter and water are in thermal equilibrium at $10.0^{\circ} \mathrm{C}$. Two metallic blocks are placed into the water. One is a $50.0-\mathrm{g}$ piece of copper at $80.0^{\circ} \mathrm{C}$. The other has a mass of 70.0 g and is originally at a temperature of $100^{\circ} \mathrm{C}$. The entire system stabilizes at a final temperature of $20.0^{\circ} \mathrm{C}$. (a) Determine the specific heat of the unknown sample. (b) Using the data in Table 20.1, can you make a positive identification of the unknown material? Can you identify a possible material? (c) Explain your answers for part (b).
12. Q|C A $3.00-\mathrm{g}$ copper coin at $25.0^{\circ} \mathrm{C}$ drops 50.0 m to the ground. (a) Assuming $60.0 \%$ of the change in gravitational potential energy of the coin-Earth system goes into increasing the internal energy of the coin, determine the coin's final temperature. (b) What If? Does the result depend on the mass of the coin? Explain.
13. Two thermally insulated vessels are connected by a narrow tube fitted with a valve that is initially closed as shown in Figure P20.13. One vessel of volume 16.8 L contains oxygen at a temperature of 300 K and a pressure of 1.75 atm . The other vessel of volume 22.4 L contains oxygen at a temperature of 450 K and a pressure of 2.25 atm . When the valve is opened, the gases in the two vessels mix and the temperature and pressure become uniform throughout. (a) What is the final temperature? (b) What is the final pressure?


Figure P20.13

## Section 20.3 Latent Heat

14. How much energy is required to change a $40.0-\mathrm{g}$ ice cube from ice at $-10.0^{\circ} \mathrm{C}$ to steam at $110^{\circ} \mathrm{C}$ ?
15. A $75.0-\mathrm{g}$ ice cube at $0^{\circ} \mathrm{C}$ is placed in 825 g of water at $25.0^{\circ} \mathrm{C}$. What is the final temperature of the mixture?
16. A $3.00-\mathrm{g}$ lead bullet at $30.0^{\circ} \mathrm{C}$ is fired at a speed of $240 \mathrm{~m} / \mathrm{s}$ into a large block of ice at $0^{\circ} \mathrm{C}$, in which it becomes embedded. What quantity of ice melts?
17. Steam at $100^{\circ} \mathrm{C}$ is added to ice at $0^{\circ} \mathrm{C}$. (a) Find the amount of ice melted and the final temperature when the mass of
steam is 10.0 g and the mass of ice is 50.0 g . (b) What If? Repeat when the mass of steam is 1.00 g and the mass of ice is 50.0 g .
18. A $1.00-\mathrm{kg}$ block of copper at $20.0^{\circ} \mathrm{C}$ is dropped into a large vessel of liquid nitrogen at 77.3 K . How many kilograms of nitrogen boil away by the time the copper reaches 77.3 K ? (The specific heat of copper is $0.0920 \mathrm{cal} / \mathrm{g} \cdot{ }^{\circ} \mathrm{C}$, and the latent heat of vaporization of nitrogen is $48.0 \mathrm{cal} / \mathrm{g}$.)
19. In an insulated vessel, 250 g of ice at $0^{\circ} \mathrm{C}$ is added to 600 g of water at $18.0^{\circ} \mathrm{C}$. (a) What is the final temperature of the system? (b) How much ice remains when the system reaches equilibrium?
20. Q|C An automobile has a mass of 1500 kg , and its aluminum brakes have an overall mass of 6.00 kg . (a) Assume all the mechanical energy that transforms into internal energy when the car stops is deposited in the brakes and no energy is transferred out of the brakes by heat. The brakes are originally at $20.0^{\circ} \mathrm{C}$. How many times can the car be stopped from $25.0 \mathrm{~m} / \mathrm{s}$ before the brakes start to melt? (b) Identify some effects ignored in part (a) that are important in a more realistic assessment of the warming of the brakes.

## Section 20.4 Work and Heat in Thermodynamic Processes

21. An ideal gas is enclosed in a cylinder with a movable piston on top of it. The piston has a mass of 8000 g and an area of $5.00 \mathrm{~cm}^{2}$ and is free to slide up and down, keeping the pressure of the gas constant. How much work is done on the gas as the temperature of 0.200 mol of the gas is raised from $20.0^{\circ} \mathrm{C}$ to $300^{\circ} \mathrm{C}$ ?
22. S An ideal gas is enclosed in a cylinder that has a movable piston on top. The piston has a mass $m$ and an area $A$ and is free to slide up and down, keeping the pressure of the gas constant. How much work is done on the gas as the temperature of $n \mathrm{~mol}$ of the gas is raised from $T_{1}$ to $T_{2}$ ?
23. An ideal gas is taken through a quasi-static process described by $P=\alpha V^{2}$, with $\alpha=5.00 \mathrm{~atm} / \mathrm{m}^{6}$, as shown in Figure P20.23. The gas is expanded to twice its original volume of $1.00 \mathrm{~m}^{3}$. How much work is done on the expanding gas


Figure P20.23 in this process?
24. (a) Determine the work done on a gas that expands from $i$ to $f$ as indicated in Figure P20.24. (b) What If? How much work is done on the gas if it is compressed from $f$ to $i$ along the same path?


Figure P20.24
25. Q|C S One mole of an ideal gas is warmed slowly so that it goes from the $P V$ state $\left(P_{i}, V_{i}\right)$ to $\left(3 P_{i}, 3 V_{i}\right)$ in such a way that the pressure of the gas is directly proportional to the volume. (a) How much work is done on the gas in the process? (b) How is the temperature of the gas related to its volume during this process?

## Section 20.5 The First Law of Thermodynamics

26. A gas is taken through the cyclic process described in Figure P20.26. (a) Find the net energy transferred to the system by heat during one complete cycle. (b) What If? If the cycle is reversed-that is, the process follows the path $A C B A$-what is the net energy input per cycle by heat?
27. Consider the cyclic process depicted in Figure P20.26. If


Figure P20.26
Problems 26 and 27. $Q$ is negative for the process $B C$ and $\Delta E_{\mathrm{int}}$ is negative for the process $C A$, what are the signs of $Q, W$, and $\Delta E_{\text {int }}$ that are associated with each of the three processes?
28. Why is the following situation impossible? An ideal gas undergoes a process with the following parameters: $Q=10.0 \mathrm{~J}$, $W=12.0 \mathrm{~J}$, and $\Delta T=-2.00^{\circ} \mathrm{C}$.
29. A thermodynamic system undergoes a process in which its internal energy decreases by 500 J . Over the same time interval, 220 J of work is done on the system. Find the energy transferred from it by heat.
30. A sample of an ideal gas goes through the process shown in Figure P20.30. From $A$ to $B$, the process is adiabatic; from $B$ to $C$, it is isobaric with 100 kJ of energy entering the system by heat; from $C$ to $D$, the process is isothermal; and from $D$ to $A$, it is isobaric with 150 kJ of energy leaving the system by heat. Determine the difference in internal energy $E_{\mathrm{int}, B}-E_{\mathrm{int}, A}$.


## Section 20.6 Some Applications of the First Law of Thermodynamics

31. An ideal gas initially at 300 K undergoes an isobaric expansion at 2.50 kPa . If the volume increases from $1.00 \mathrm{~m}^{3}$ to $3.00 \mathrm{~m}^{3}$ and 12.5 kJ is transferred to the gas by heat, what are (a) the change in its internal energy and (b) its final temperature?
32. (a) How much work is done on the steam when 1.00 mol of water at $100^{\circ} \mathrm{C}$ boils and becomes 1.00 mol of steam at $100^{\circ} \mathrm{C}$ at 1.00 atm pressure? Assume the steam to behave as an ideal gas. (b) Determine the change in internal
energy of the system of the water and steam as the water vaporizes.
33. M A $2.00-\mathrm{mol}$ sample of helium gas initially at 300 K , and 0.400 atm is compressed isothermally to 1.20 atm . Noting that the helium behaves as an ideal gas, find (a) the final volume of the gas, (b) the work done on the gas, and (c) the energy transferred by heat.
34. One mole of an ideal gas does 3000 J of work on its surroundings as it expands isothermally to a final pressure of 1.00 atm and volume of 25.0 L . Determine (a) the initial volume and (b) the temperature of the gas.
35. An ideal gas initially at $P_{i}, V_{i}$, and $T_{i}$ is taken through a cycle as shown in Figure P20.35. (a) Find the net work done on the gas per cycle for 1.00 mol of gas initially at $0^{\circ} \mathrm{C}$. (b) What is the net energy added by heat to the gas per cycle?
36. S An ideal gas initially at $P_{i}, V_{i}$, and $T_{i}$ is taken through a cycle as shown in Figure


Figure P20.35
Problems 35 and 36. P20.35. (a) Find the net work done on the gas per cycle. (b) What is the net energy added by heat to the system per cycle?
37. A $1.00-\mathrm{kg}$ block of aluminum is warmed at atmospheric pressure so that its temperature increases from $22.0^{\circ} \mathrm{C}$ to $40.0^{\circ} \mathrm{C}$. Find (a) the work done on the aluminum, (b) the energy added to it by heat, and (c) the change in its internal energy.
38. In Figure P20.38, the change in internal energy of a gas that is taken from $A$ to $C$ along the blue path is +800 J . The work done on the gas along the red path $A B C$ is -500 J . (a) How much energy must be added to the system by heat as it goes from $A$ through $B$ to $C$ ? (b) If the pressure at point $A$ is five times that of point $C$, what is the work done on the system in going from $C$ to


Figure P20.38 $D$ ? (c) What is the energy exchanged with the surroundings by heat as the gas goes from $C$ to $A$ along the green path? (d) If the change in internal energy in going from point $D$ to point $A$ is +500 J , how much energy must be added to the system by heat as it goes from point $C$ to point $D$ ?

## Section 20.7 Energy Transfer Mechanisms in Thermal Processes

39. A glass windowpane in a home is 0.620 cm thick and has dimensions of $1.00 \mathrm{~m} \times 2.00 \mathrm{~m}$. On a certain day, the temperature of the interior surface of the glass is $25.0^{\circ} \mathrm{C}$ and the exterior surface temperature is $0^{\circ} \mathrm{C}$. (a) What is the rate at which energy is transferred by heat through the glass? (b) How much energy is transferred through the window in one day, assuming the temperatures on the surfaces remain constant?
40. A concrete slab is 12.0 cm thick and has an area of $5.00 \mathrm{~m}^{2}$. Electric heating coils are installed under the slab to melt the ice on the surface in the winter months. What mini-
mum power must be supplied to the coils to maintain a temperature difference of $20.0^{\circ} \mathrm{C}$ between the bottom of the slab and its surface? Assume all the energy transferred is through the slab.
41. A student is trying to decide what to wear. His bedroom is at $20.0^{\circ} \mathrm{C}$. His skin temperature is $35.0^{\circ} \mathrm{C}$. The area of his exposed skin is $1.50 \mathrm{~m}^{2}$. People all over the world have skin that is dark in the infrared, with emissivity about 0.900 . Find the net energy transfer from his body by radiation in 10.0 min .
42. The surface of the Sun has a temperature of about 5800 K . The radius of the Sun is $6.96 \times 10^{8} \mathrm{~m}$. Calculate the total energy radiated by the Sun each second. Assume the emissivity of the Sun is 0.986 .
43. The tungsten filament of a certain $100-\mathrm{W}$ lightbulb radiates 2.00 W of light. (The other 98 W is carried away by convection and conduction.) The filament has a surface area of $0.250 \mathrm{~mm}^{2}$ and an emissivity of 0.950 . Find the filament's temperature. (The melting point of tungsten is 3683 K .)
44. At high noon, the Sun delivers 1000 W to each square meter of a blacktop road. If the hot asphalt transfers energy only by radiation, what is its steady-state temperature?
45. Two lightbulbs have cylindrical filaments much greater in length than in diameter. The evacuated bulbs are identical except that one operates at a filament temperature of $2100^{\circ} \mathrm{C}$ and the other operates at $2000^{\circ} \mathrm{C}$. (a) Find the ratio of the power emitted by the hotter lightbulb to that emitted by the cooler lightbulb. (b) With the bulbs operating at the same respective temperatures, the cooler lightbulb is to be altered by making its filament thicker so that it emits the same power as the hotter one. By what factor should the radius of this filament be increased?
46. $\mathbf{Q} \mid \mathbf{C}$ At our distance from the Sun, the intensity of solar radiation is $1370 \mathrm{~W} / \mathrm{m}^{2}$. The temperature of the Earth is affected by the greenhouse effect of the atmosphere. This phenomenon describes the effect of absorption of infrared light emitted by the surface so as to make the surface temperature of the Earth higher than if it were airless. For comparison, consider a spherical object of radius $r$ with no atmosphere at the same distance from the Sun as the Earth. Assume its emissivity is the same for all kinds of electromagnetic waves and its temperature is uniform over its surface. (a) Explain why the projected area over which it absorbs sunlight is $\pi r^{2}$ and the surface area over which it radiates is $4 \pi r^{2}$. (b) Compute its steady-state temperature. Is it chilly?
47. (a) Calculate the $R$-value of a thermal window made of two single panes of glass each 0.125 in. thick and separated by a $0.250-\mathrm{in}$. air space. (b) By what factor is the transfer of energy by heat through the window reduced by using the thermal window instead of the single-pane window? Include the contributions of inside and outside stagnant air layers.
48. Q|C For bacteriological testing of water supplies and in medical clinics, samples must routinely be incubated for 24 h at $37^{\circ} \mathrm{C}$. Peace Corps volunteer and MIT engineer Amy Smith invented a low-cost, low-maintenance incubator. The incubator consists of a foam-insulated box containing
a waxy material that melts at $37.0^{\circ} \mathrm{C}$ interspersed among tubes, dishes, or bottles containing the test samples and growth medium (bacteria food). Outside the box, the waxy material is first melted by a stove or solar energy collector. Then the waxy material is put into the box to keep the test samples warm as the material solidifies. The heat of fusion of the phase-change material is $205 \mathrm{~kJ} / \mathrm{kg}$. Model the insulation as a panel with surface area $0.490 \mathrm{~m}^{2}$, thickness 4.50 cm , and conductivity $0.0120 \mathrm{~W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$. Assume the exterior temperature is $23.0^{\circ} \mathrm{C}$ for 12.0 h and $16.0^{\circ} \mathrm{C}$ for 12.0 h . (a) What mass of the waxy material is required to conduct the bacteriological test? (b) Explain why your calculation can be done without knowing the mass of the test samples or of the insulation.
49. A bar of gold (Au) is in thermal contact with a bar of silver ( Ag ) of the same length and area (Fig. P20.49). One end of the compound bar is maintained at $80.0^{\circ} \mathrm{C}$, and the opposite end is at $30.0^{\circ} \mathrm{C}$. When the energy transfer reaches steady state, what is the temperature at the junction?
50. A large, hot pizza floats in outer space after being jettisoned as


Figure P20.49 refuse from a spacecraft. What is the order of magnitude (a) of its rate of energy loss and (b) of its rate of temperature change? List the quantities you estimate and the value you estimate for each.

## Additional Problems

51. Liquid nitrogen has a boiling point of 77.3 K and a latent heat of vaporization of $2.01 \times 10^{5} \mathrm{~J} / \mathrm{kg}$. A $25.0-\mathrm{W}$ electric heating element is immersed in an insulated vessel containing 25.0 L of liquid nitrogen at its boiling point. How many kilograms of nitrogen are boiled away in a period of 4.00 h ?
52. GP Review. Two speeding lead bullets, one of mass 12.0 g moving to the right at $300 \mathrm{~m} / \mathrm{s}$ and one of mass 8.00 g moving to the left at $400 \mathrm{~m} / \mathrm{s}$, collide head-on, and all the material sticks together. Both bullets are originally at temperature $30.0^{\circ} \mathrm{C}$. Assume the change in kinetic energy of the system appears entirely as increased internal energy. We would like to determine the temperature and phase of the bullets after the collision. (a) What two analysis models are appropriate for the system of two bullets for the time interval from before to after the collision? (b) From one of these models, what is the speed of the combined bullets after the collision? (c) How much of the initial kinetic energy has transformed to internal energy in the system after the collision? (d) Does all the lead melt due to the collision? (e) What is the temperature of the combined bullets after the collision? (f) What is the phase of the combined bullets after the collision?
53. M An aluminum rod 0.500 m in length and with a crosssectional area of $2.50 \mathrm{~cm}^{2}$ is inserted into a thermally insulated vessel containing liquid helium at 4.20 K . The rod is initially at 300 K . (a) If one-half of the rod is inserted into the helium, how many liters of helium boil off by the time the inserted half cools to 4.20 K ? Assume the upper half
does not yet cool. (b) If the circular surface of the upper end of the rod is maintained at 300 K , what is the approximate boil-off rate of liquid helium in liters per second after the lower half has reached 4.20 K ? (Aluminum has thermal conductivity of $3100 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ at 4.20 K ; ignore its temperature variation. The density of liquid helium is $125 \mathrm{~kg} / \mathrm{m}^{3}$.)
54. Q|C An ice-cube tray is filled with 75.0 g of water. After the filled tray reaches an equilibrium temperature of $20.0^{\circ} \mathrm{C}$, it is placed in a freezer set at $-8.00^{\circ} \mathrm{C}$ to make ice cubes. (a) Describe the processes that occur as energy is being removed from the water to make ice. (b) Calculate the energy that must be removed from the water to make ice cubes at $-8.00^{\circ} \mathrm{C}$.
55. A flow calorimeter is an apparatus used to measure the specific heat of a liquid. The technique of flow calorimetry involves measuring the temperature difference between the input and output points of a flowing stream of the liquid while energy is added by heat at a known rate. A liquid of density $900 \mathrm{~kg} / \mathrm{m}^{3}$ flows through the calorimeter with volume flow rate of $2.00 \mathrm{~L} / \mathrm{min}$. At steady state, a temperature difference $3.50^{\circ} \mathrm{C}$ is established between the input and output points when energy is supplied at the rate of 200 W . What is the specific heat of the liquid?
56. S A flow calorimeter is an apparatus used to measure the specific heat of a liquid. The technique of flow calorimetry involves measuring the temperature difference between the input and output points of a flowing stream of the liquid while energy is added by heat at a known rate. A liquid of density $\rho$ flows through the calorimeter with volume flow rate $R$. At steady state, a temperature difference $\Delta T$ is established between the input and output points when energy is supplied at the rate $P$. What is the specific heat of the liquid?
57. Review. Following a collision between a large spacecraft and an asteroid, a copper disk of radius 28.0 m and thickness 1.20 m at a temperature of $850^{\circ} \mathrm{C}$ is floating in space, rotating about its symmetry axis with an angular speed of $25.0 \mathrm{rad} / \mathrm{s}$. As the disk radiates infrared light, its temperature falls to $20.0^{\circ} \mathrm{C}$. No external torque acts on the disk. (a) Find the change in kinetic energy of the disk. (b) Find the change in internal energy of the disk. (c) Find the amount of energy it radiates.
58. $\mathbf{Q} \mid \mathbf{C}$ One mole of an ideal gas is contained in a cylinder with a movable piston. The initial pressure, volume, and temperature are $P_{i}, V_{i}$, and $T_{i}$, respectively. Find the work done on the gas in the following processes. In operational terms, describe how to carry out each process and show each process on a $P V$ diagram. (a) an isobaric compression in which the final volume is one-half the initial volume (b) an isothermal compression in which the final pressure is four times the initial pressure (c) an isovolumetric process in which the final pressure is three times the initial pressure
59. Review. A $670-\mathrm{kg}$ meteoroid happens to be composed of aluminum. When it is far from the Earth, its temperature is $-15.0^{\circ} \mathrm{C}$ and it moves at $14.0 \mathrm{~km} / \mathrm{s}$ relative to the planet. As it crashes into the Earth, assume the internal energy transformed from the mechanical energy of the meteoroid-

Earth system is shared equally between the meteoroid and the Earth and all the material of the meteoroid rises momentarily to the same final temperature. Find this temperature. Assume the specific heat of liquid and of gaseous aluminum is $1170 \mathrm{~J} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}$.
60. Why is the following situation impossible? A group of campers arises at 8:30 a.m. and uses a solar cooker, which consists of a curved, reflecting surface that concentrates sunlight onto the object to be warmed (Fig. P20.60). During the day, the maximum solar intensity reaching the Earth's surface at the cooker's location is $I=600 \mathrm{~W} / \mathrm{m}^{2}$. The


Figure P20.60 cooker faces the Sun and has a face diameter of $d=0.600 \mathrm{~m}$. Assume a fraction $f$ of $40.0 \%$ of the incident energy is transferred to 1.50 L of water in an open container, initially at $20.0^{\circ} \mathrm{C}$. The water comes to a boil, and the campers enjoy hot coffee for breakfast before hiking ten miles and returning by noon for lunch.
61. M Water in an electric teakettle is boiling. The power absorbed by the water is 1.00 kW . Assuming the pressure of vapor in the kettle equals atmospheric pressure, determine the speed of effusion of vapor from the kettle's spout if the spout has a cross-sectional area of $2.00 \mathrm{~cm}^{2}$. Model the steam as an ideal gas.
62. (a) In air at $0^{\circ} \mathrm{C}$, a $1.60-\mathrm{kg}$ copper block at $0^{\circ} \mathrm{C}$ is set sliding at $2.50 \mathrm{~m} / \mathrm{s}$ over a sheet of ice at $0^{\circ} \mathrm{C}$. Friction brings the block to rest. Find the mass of the ice that melts. (b) As the block slows down, identify its energy input $Q$, its change in internal energy $\Delta E_{\text {int, }}$, and the change in mechanical energy for the block-ice system. (c) For the ice as a system, identify its energy input $Q$ and its change in internal energy $\Delta E_{\text {int }}$. (d) A $1.60-\mathrm{kg}$ block of ice at $0^{\circ} \mathrm{C}$ is set sliding at $2.50 \mathrm{~m} / \mathrm{s}$ over a sheet of copper at $0^{\circ} \mathrm{C}$. Friction brings the block to rest. Find the mass of the ice that melts. (e) Evaluate $Q$ and $\Delta E_{\text {int }}$ for the block of ice as a system and $\Delta E_{\text {mech }}$ for the block-ice system. (f) Evaluate $Q$ and $\Delta E_{\text {int }}$ for the metal sheet as a system. (g) A thin, $1.60-\mathrm{kg}$ slab of copper at $20^{\circ} \mathrm{C}$ is set sliding at $2.50 \mathrm{~m} / \mathrm{s}$ over an identical stationary slab at the same temperature. Friction quickly stops the motion. Assuming no energy is transferred to the environment by heat, find the change in temperature of both objects. (h) Evaluate $Q$ and $\Delta E_{\text {int }}$ for the sliding slab and $\Delta E_{\text {mech }}$ for the two-slab system. (i) Evaluate $Q$ and $\Delta E_{\mathrm{int}}$ for the stationary slab.
63. A cooking vessel on a slow burner contains 10.0 kg of water and an unknown mass of ice in equilibrium at $0^{\circ} \mathrm{C}$ at time $t=0$. The temperature of the mixture is measured at various times, and the result is plotted in Figure P20.63. During the first 50.0 min ,


Figure P20.63
the mixture remains at $0^{\circ} \mathrm{C}$. From 50.0 min to 60.0 min , the temperature increases to $2.00^{\circ} \mathrm{C}$. Ignoring the heat capacity of the vessel, determine the initial mass of the ice.
64. The average thermal conductivity of the walls (including the windows) and roof of the house depicted in Figure P20.64 is $0.480 \mathrm{~W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$, and their average thickness is 21.0 cm . The house is kept warm with natural gas having a heat of combustion (that is, the energy provided per cubic meter of gas burned) of $9300 \mathrm{kcal} / \mathrm{m}^{3}$. How many cubic meters of gas must be burned each day to maintain an inside temperature of $25.0^{\circ} \mathrm{C}$ if the outside temperature is $0.0^{\circ} \mathrm{C}$ ? Disregard radiation and the energy transferred by heat through the ground.


Figure P20.64
65. Q|C During periods of high activity, the Sun has more sunspots than usual. Sunspots are cooler than the rest of the luminous layer of the Sun's atmosphere (the photosphere). Paradoxically, the total power output of the active Sun is not lower than average but is the same or slightly higher than average. Work out the details of the following crude model of this phenomenon. Consider a patch of the photosphere with an area of $5.10 \times 10^{14} \mathrm{~m}^{2}$. Its emissivity is 0.965 . (a) Find the power it radiates if its temperature is uniformly 5800 K , corresponding to the quiet Sun. (b) To represent a sunspot, assume $10.0 \%$ of the patch area is at 4800 K and the other $90.0 \%$ is at 5890 K . Find the power output of the patch. (c) State how the answer to part (b) compares with the answer to part (a). (d) Find the average temperature of the patch. Note that this cooler temperature results in a higher power output. (The next sunspot maximum is expected around the year 2012.)
66. Q|C A student measures the following data in a calorimetry experiment designed to determine the specific heat of aluminum:

| Initial temperature of water |  |
| :--- | :---: |
| $\quad$ and calorimeter: | $70.0^{\circ} \mathrm{C}$ |
| Mass of water: | 0.400 kg |
| Mass of calorimeter: | 0.040 kg |
| Specific heat of calorimeter: | $0.63 \mathrm{~kJ} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}$ |
| Initial temperature of aluminum: | $27.0^{\circ} \mathrm{C}$ |
| Mass of aluminum: | 0.200 kg |
| Final temperature of mixture: | $66.3^{\circ} \mathrm{C}$ |

(a) Use these data to determine the specific heat of aluminum. (b) Explain whether your result is within $15 \%$ of the value listed in Table 20.1.

## Challenge Problems

67. A pond of water at $0^{\circ} \mathrm{C}$ is covered with a layer of ice 4.00 cm thick. If the air temperature stays constant at $-10.0^{\circ} \mathrm{C}$, what time interval is required for the ice thickness to increase to 8.00 cm ? Suggestion: Use Equation 20.16 in the form

$$
\frac{d Q}{d t}=k A \frac{\Delta T}{x}
$$

and note that the incremental energy $d Q$ extracted from the water through the thickness $x$ of ice is the amount required to freeze a thickness $d x$ of ice. That is, $d Q=$ $L_{f} \rho A d x$, where $\rho$ is the density of the ice, $A$ is the area, and $L_{f}$ is the latent heat of fusion.
68. (a) The inside of a hollow cylinder is maintained at a temperature $T_{a}$, and the outside is at a lower temperature, $T_{b}$ (Fig. P20.68). The wall of the cylinder has a thermal conductivity $k$. Ignoring end effects, show that the rate of energy conduction from the inner surface to the outer surface in the radial direction is

$$
\frac{d Q}{d t}=2 \pi L k\left[\frac{T_{a}-T_{b}}{\ln (b / a)}\right]
$$



Figure P20.68

Suggestions: The temperature gradient is $d T / d r$. A radial energy current passes through a concentric cylinder of area $2 \pi r L$. (b) The passenger section of a jet airliner is in the shape of a cylindrical tube with a length of 35.0 m and an inner radius of 2.50 m . Its walls are lined with an insulating material 6.00 cm in thickness and having a thermal conductivity of $4.00 \times 10^{-5} \mathrm{cal} / \mathrm{s} \cdot \mathrm{cm} \cdot{ }^{\circ} \mathrm{C}$. A heater must maintain the interior temperature at $25.0^{\circ} \mathrm{C}$ while the outside temperature is $-35.0^{\circ} \mathrm{C}$. What power must be supplied to the heater?
69. Consider the piston-cylinder apparatus shown in Figure P20.69. The bottom of the cylinder contains 2.00 kg of water at just under $100.0^{\circ} \mathrm{C}$. The cylinder has a radius of $r=7.50 \mathrm{~cm}$. The piston of mass $m=3.00 \mathrm{~kg}$ sits on the
surface of the water. An electric heater in the cylinder base transfers energy into the water at a rate of 100 W. Assume the cylinder is much taller than shown in the figure, so we don't need to be concerned about the piston reaching the top of the cylinder. (a) Once the water begins boiling, how


Figure P20.69 fast is the piston rising? Model the steam as an ideal gas. (b) After the water has completely turned to steam and the heater continues to transfer energy to the steam at the same rate, how fast is the piston rising?
70. $\mathbf{Q} \mid \mathbf{C}$ A spherical shell has inner radius 3.00 cm and outer radius 7.00 cm . It is made of material with thermal conductivity $k=0.800 \mathrm{~W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$. The interior is maintained at temperature $5^{\circ} \mathrm{C}$ and the exterior at $40^{\circ} \mathrm{C}$. After an interval of time, the shell reaches a steady state with the temperature at each point within it remaining constant in time. (a) Explain why the rate of energy transfer $P$ must be the same through each spherical surface, of radius $r$, within the shell and must satisfy

$$
\frac{d T}{d r}=\frac{P}{4 \pi k r^{2}}
$$

(b) Next, prove that

$$
\int_{5}^{40} d T=\frac{P}{4 \pi k} \int_{0.03}^{0.07} r^{-2} d r
$$

where $T$ is in degrees Celsius and $r$ is in meters. (c) Find the rate of energy transfer through the shell. (d) Prove that

$$
\int_{5}^{T} d T=1.84 \int_{0.03}^{r} r^{-2} d r
$$

where $T$ is in degrees Celsius and $r$ is in meters. (e) Find the temperature within the shell as a function of radius. (f) Find the temperature at $r=5.00 \mathrm{~cm}$, halfway through the shell.

