Chapter 23

Electric Fields



Electricity and Magnetism, Some History



- Many applications
 - Macroscopic and microscopic
- Chinese
 - Documents suggest that magnetism was observed as early as 2000 BC
- Greeks
 - Electrical and magnetic phenomena as early as 700 BC
 - Experiments with amber and magnetite

Electricity and Magnetism, Some History, 2



- 1600
 - William Gilbert showed electrification effects were not confined to just amber
 - The electrification effects were a general phenomena
- 1785
 - Charles Coulomb confirmed inverse square law form for electric forces

Electricity and Magnetism, Some History, 3



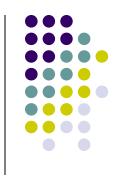
- 1819
 - Hans Oersted found a compass needle deflected when near a wire carrying an electric current
- 1831
 - Michael Faraday and Joseph Henry showed that when a wire is moved near a magnet, an electric current is produced in the wire

Electricity and Magnetism, Some History, 4



- 1873
 - James Clerk Maxwell used observations and other experimental facts as a basis for formulating the laws of electromagnetism
 - Unified electricity and magnetism
- 1888
 - Heinrich Hertz verified Maxwell's predictions
 - He produced electromagnetic waves

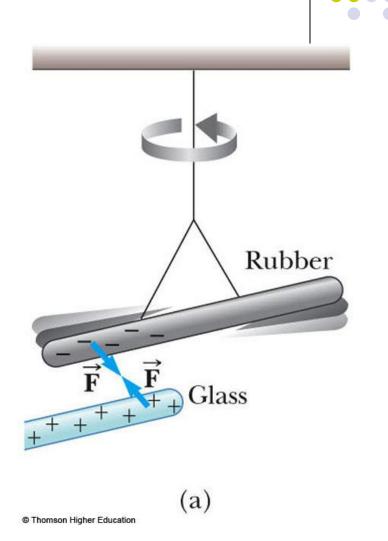
Electric Charges



- There are two kinds of electric charges
 - Called positive and negative
 - Negative charges are the type possessed by electrons
 - Positive charges are the type possessed by protons
- Charges of the same sign repel one another and charges with opposite signs attract one another

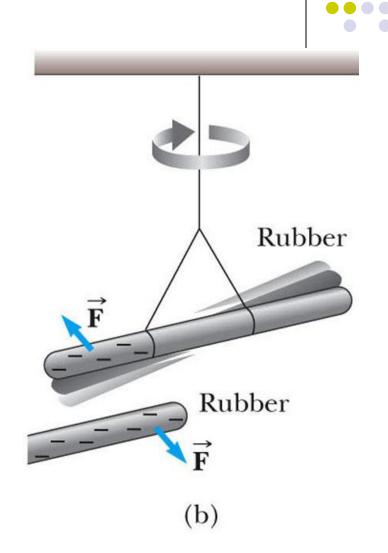
Electric Charges, 2

- The rubber rod is negatively charged
- The glass rod is positively charged
- The two rods will attract

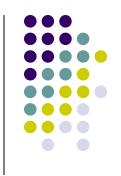


Electric Charges, 3

- The rubber rod is negatively charged
- The second rubber rod is also negatively charged
- The two rods will repel



More About Electric Charges

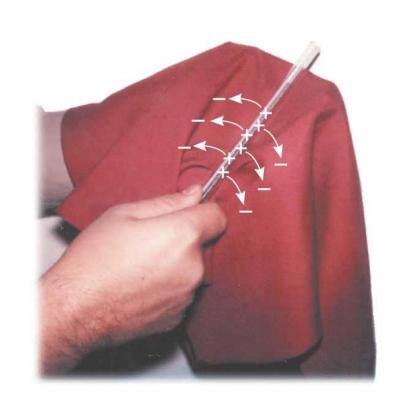


- Electric charge is always conserved in an isolated system
 - For example, charge is not created in the process of rubbing two objects together
 - The electrification is due to a transfer of charge from one object to another

Conservation of Electric Charges



- A glass rod is rubbed with silk
- Electrons are transferred from the glass to the silk
- Each electron adds a negative charge to the silk
- An equal positive charge is left on the rod



Quantization of Electric Charges



- The electric charge, q, is said to be quantized
 - q is the standard symbol used for charge as a variable
 - Electric charge exists as discrete packets
 - $q = \pm Ne$
 - N is an integer
 - e is the fundamental unit of charge
 - $|e| = 1.6 \times 10^{-19} \text{ C}$
 - Electron: q = -e
 - Proton: q = +e

Conductors



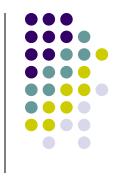
- Electrical conductors are materials in which some of the electrons are free electrons
 - Free electrons are not bound to the atoms
 - These electrons can move relatively freely through the material
 - Examples of good conductors include copper, aluminum and silver
 - When a good conductor is charged in a small region, the charge readily distributes itself over the entire surface of the material

Insulators



- Electrical insulators are materials in which all of the electrons are bound to atoms
 - These electrons can not move relatively freely through the material
 - Examples of good insulators include glass, rubber and wood
 - When a good insulator is charged in a small region, the charge is unable to move to other regions of the material

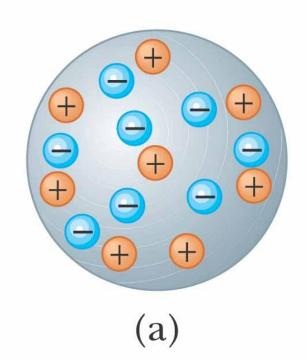
Semiconductors



- The electrical properties of semiconductors are somewhere between those of insulators and conductors
- Examples of semiconductor materials include silicon and germanium

Charging by Induction

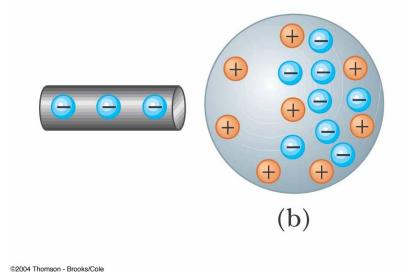
- Charging by induction requires no contact with the object inducing the charge
- Assume we start with a neutral metallic sphere
 - The sphere has the same number of positive and negative charges



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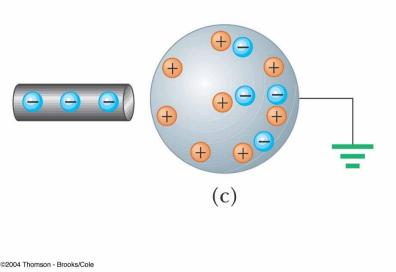
Charging by Induction, 2

- A charged rubber rod is placed near the sphere
 - It does **not** touch the sphere
- The electrons in the neutral sphere are redistributed



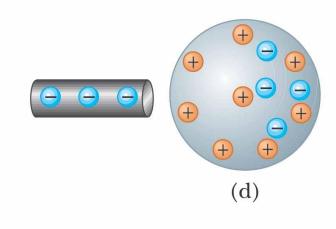


- The sphere is grounded
- Some electrons can leave the sphere through the ground wire



Charging by Induction, 4

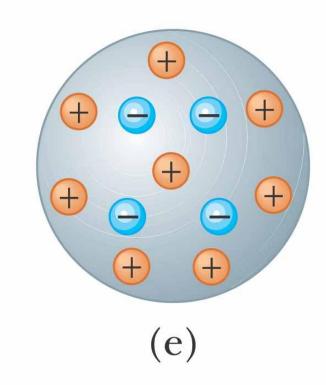
- The ground wire is removed
- There will now be more positive charges
- The charges are not uniformly distributed
- The positive charge has been *induced* in the sphere



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Charging by Induction, 5

- The rod is removed
- The electrons remaining on the sphere redistribute themselves
- There is still a net positive charge on the sphere
- The charge is now uniformly distributed

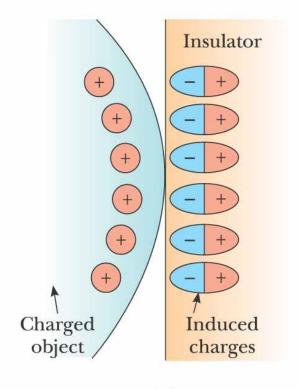


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Charge Rearrangement in Insulators



- A process similar to induction can take place in insulators
- The charges within the molecules of the material are rearranged

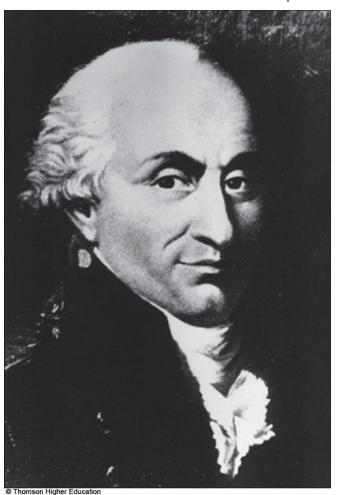


(a)

Charles Coulomb

- 1736 1806
- French physicist
- Major contributions were in areas of electrostatics and magnetism
- Also investigated in areas of
 - Strengths of materials
 - Structural mechanics
 - **Ergonomics**

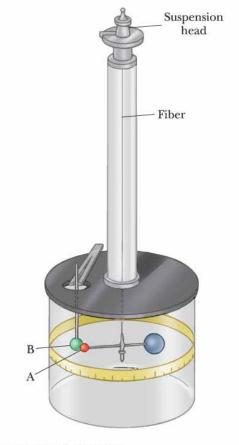




Coulomb's Law

- Charles Coulomb measured the magnitudes of electric forces between two small charged spheres
- He found the force depended on the charges and the distance between them





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Point Charge



- The term point charge refers to a particle of zero size that carries an electric charge
 - The electrical behavior of electrons and protons is well described by modeling them as point charges

Coulomb's Law, 2



- The electrical force between two stationary point charges is given by Coulomb's Law
- The force is inversely proportional to the square of the separation r between the charges and directed along the line joining them
- The force is proportional to the product of the charges, q_1 and q_2 , on the two particles

Coulomb's Law, 3



- The force is attractive if the charges are of opposite sign
- The force is repulsive if the charges are of like sign
- The force is a conservative force

Coulomb's Law, Equation



Mathematically,

$$F_{e} = k_{e} \frac{\left|q_{1}\right|\left|q_{2}\right|}{r^{2}}$$

- The SI unit of charge is the coulomb (C)
- k_{P} is called the **Coulomb constant**
 - $k_e = 8.9876 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2 = 1/(4\pi e_0)$
 - e_0 is the **permittivity of free space**
 - $e_0 = 8.8542 \times 10^{-12} \text{ C}^2 / \text{ N} \cdot \text{m}^2$

Coulomb's Law, Notes



- Remember the charges need to be in coulombs
 - e is the smallest unit of charge
 - except quarks
 - $e = 1.6 \times 10^{-19} \text{ C}$
 - So 1 C needs 6.24 x 10¹⁸ electrons or protons
- Typical charges can be in the µC range
- Remember that force is a vector quantity





TABLE 23.1

Charge and Mass of the Electron, Proton, and Neutron

Particle	Charge (C)	Mass (kg)
Electron (e)	$-1.602\ 176\ 5 \times 10^{-19}$	$9.109 \ 4 \times 10^{-31}$
Proton (p)	$+1.602\ 176\ 5 \times 10^{-19}$	$1.672 62 \times 10^{-27}$
Neutron (n)	0	1.67493×10^{-27}

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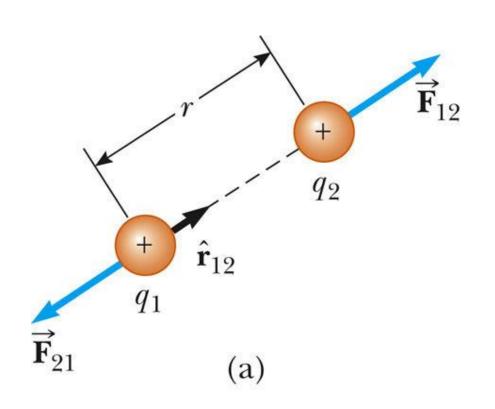
Vector Nature of Electric Forces



In vector form,

$$\vec{\mathbf{F}}_{12} = k_{\rm e} \frac{q_1 q_2}{r^2} \hat{\mathbf{r}}_{12}$$

- \hat{r}_{12} is a unit vector directed from q_1 to q_2
- The like charges produce a repulsive force between them
- Use the active figure to move the charges and observe the force



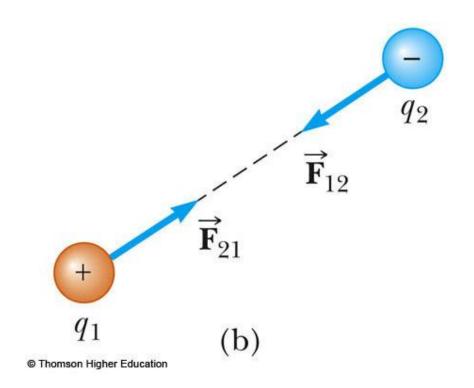
Vector Nature of Electrical Forces, 2



- Electrical forces obey Newton's Third Law
- The force on q₁ is equal in magnitude and opposite in direction to the force on q₂
 - $\vec{F}_{21} = -\vec{F}_{12}$
- With like signs for the charges, the product q_1q_2 is positive and the force is repulsive

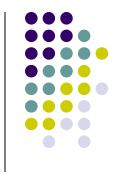
Vector Nature of Electrical Forces, 3

- Two point charges are separated by a distance r
- The unlike charges produce an attractive force between them
- With unlike signs for the charges, the product q₁q₂ is negative and the force is attractive
 - Use the active figure to investigate the force for different positions





A Final Note about Directions



- The sign of the product of q_1q_2 gives the relative direction of the force between q_1 and q_2
- The absolute direction is determined by the actual location of the charges





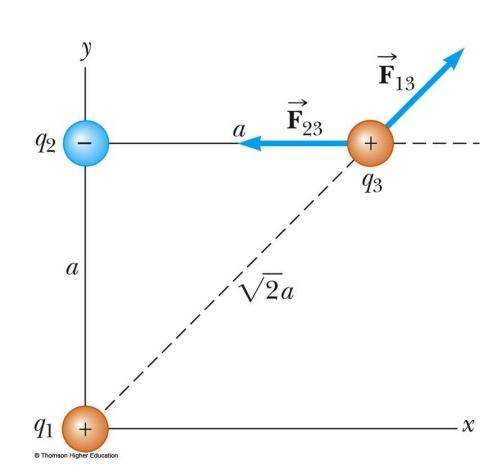
- The resultant force on any one charge equals the vector sum of the forces exerted by the other individual charges that are present
 - Remember to add the forces as vectors
- The resultant force on q_1 is the vector sum of all the forces exerted on it by other charges:

$$\vec{F}_1 = \vec{F}_{21} + \vec{F}_{31} + \vec{F}_{41}$$

Superposition Principle, Example

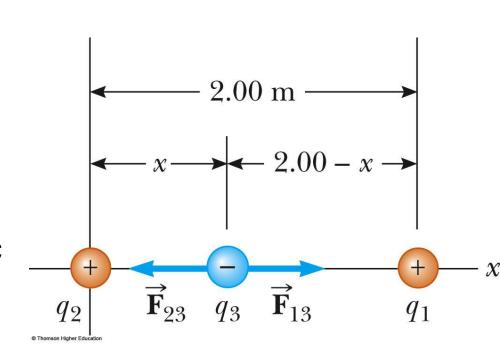


- The force exerted by q_1 on q_3 is $\vec{\mathbf{f}}_{13}$
- The force exerted by q_2 on q_3 is $\vec{\mathbf{F}}_{23}$
- The resultant force exerted on q_3 is the vector sum of $\vec{\mathbf{F}}_{13}$ and $\vec{\mathbf{F}}_{23}$



Zero Resultant Force, Example

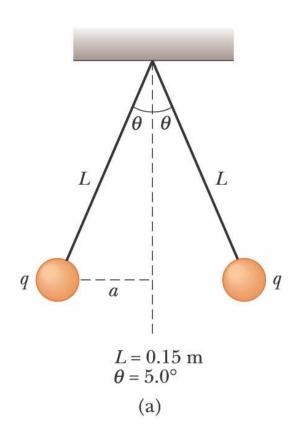
- Where is the resultant force equal to zero?
 - The magnitudes of the individual forces will be equal
 - Directions will be opposite
- Will result in a quadratic
- Choose the root that gives the forces in opposite directions



Electrical Force with Other Forces, Example

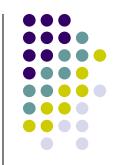


- The spheres are in equilibrium
- Since they are separated, they exert a repulsive force on each other
 - Charges are like charges
- Proceed as usual with equilibrium problems, noting one force is an electrical force

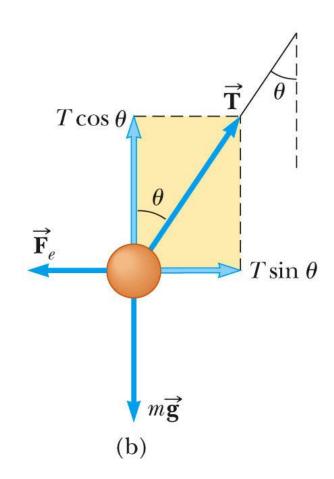


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Electrical Force with Other Forces, Example cont.



- The free body diagram includes the components of the tension, the electrical force, and the weight
- Solve for |q|
- You cannot determine the sign of q, only that they both have same sign



Electric Field – Introduction



- The electric force is a field force
- Field forces can act through space
 - The effect is produced even with no physical contact between objects
- Faraday developed the concept of a field in terms of electric fields

Electric Field – Definition



- An electric field is said to exist in the region of space around a charged object
 - This charged object is the source charge
- When another charged object, the test charge, enters this electric field, an electric force acts on it





- The electric field is defined as the electric force on the test charge per unit charge
- The electric field vector, $\vec{\mathbf{E}}$, at a point in space is defined as the electric force $\vec{\mathbf{F}}$ acting on a positive test charge, q_0 placed at that point divided by the test charge:

$$\vec{\mathsf{E}}\equivrac{\mathsf{F}}{q_{_{\mathrm{O}}}}$$

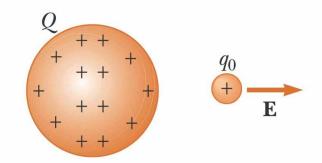
Electric Field, Notes



- **E** is the field produced by some charge or charge distribution, separate from the test charge
- The existence of an electric field is a property of the source charge
 - The presence of the test charge is not necessary for the field to exist
- The test charge serves as a detector of the field

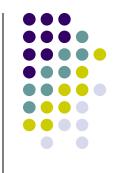
Electric Field Notes, Final

- The direction of **E** is that of the force on a positive test charge
- The SI units of **E** are N/C
- We can also say that an electric field exists at a point if a test charge at that point experiences an electric force



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Relationship Between F and E



- $\bullet \ \vec{\mathsf{F}}_e = q\vec{\mathsf{E}}$
 - This is valid for a point charge only
 - One of zero size
 - For larger objects, the field may vary over the size of the object
- If q is positive, the force and the field are in the same direction
- If q is negative, the force and the field are in opposite directions





 Remember Coulomb's law, between the source and test charges, can be expressed as

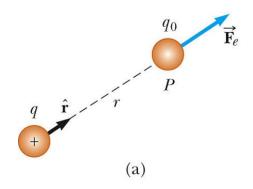
$$\vec{\mathbf{F}}_{e} = k_{e} \frac{qq_{o}}{r^{2}} \hat{\mathbf{r}}$$

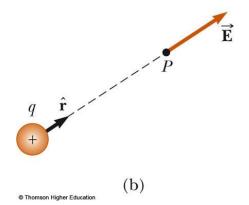
Then, the electric field will be

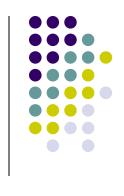
$$\vec{\mathbf{E}} = \frac{\vec{\mathbf{F}}_{e}}{q_{o}} = k_{e} \frac{q}{r^{2}} \hat{\mathbf{r}}$$

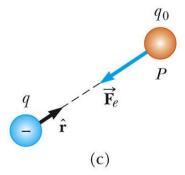
More About Electric Field Direction

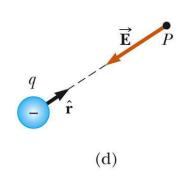
- a) q is positive, the force is directed away from q
- b) The direction of the field is also away from the positive source charge
- c) q is negative, the force is directed toward q
- d) The field is also toward the negative source charge
- Use the active figure to change the position of point P and observe the electric field





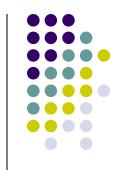








Superposition with Electric Fields

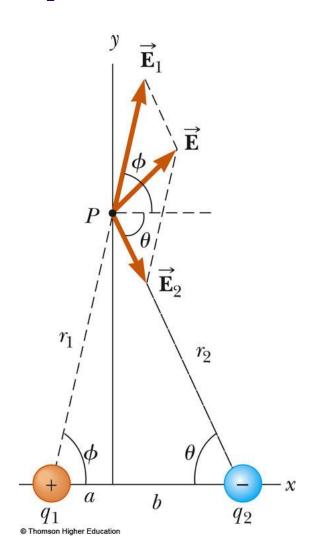


 At any point P, the total electric field due to a group of source charges equals the vector sum of the electric fields of all the charges

$$\vec{\mathbf{E}} = k_{\rm e} \sum_{i} \frac{q_{i}}{r_{i}^{2}} \hat{\mathbf{r}}_{i}$$

Superposition Example

- Find the electric field due to q_1 , \vec{E}_1
- Find the electric field due to q_2 , $\vec{\mathbf{E}}_2$
- $\bullet \quad \vec{\mathbf{E}} = \vec{\mathbf{E}}_1 + \vec{\mathbf{E}}_2$
 - Remember, the fields add as vectors
 - The direction of the individual fields is the direction of the force on a positive test charge



Electric Field – Continuous Charge Distribution



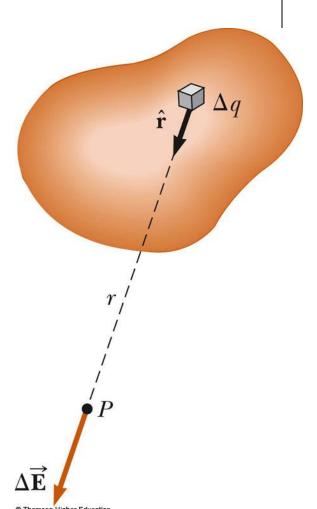
- The distances between charges in a group of charges may be much smaller than the distance between the group and a point of interest
- In this situation, the system of charges can be modeled as continuous
- The system of closely spaced charges is equivalent to a total charge that is continuously distributed along some line, over some surface, or throughout some volume

Electric Field – Continuous Charge Distribution, cont



Procedure:

- Divide the charge distribution into small elements, each of which contains Δq
- Calculate the electric field due to one of these elements at point P
- Evaluate the total field by summing the contributions of all the charge elements



Electric Field – Continuous Charge Distribution, equations



For the individual charge elements

$$\Delta \vec{\mathbf{E}} = k_e \frac{\Delta q}{r^2} \hat{\mathbf{r}}$$

Because the charge distribution is continuous

$$\vec{\mathbf{E}} = k_e \lim_{\Delta q_i \to 0} \sum_{i} \frac{\Delta q_i}{r_i^2} \hat{\mathbf{r}}_i = k_e \int \frac{dq}{r^2} \hat{\mathbf{r}}$$

Charge Densities

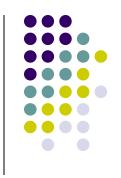
- Volume charge density: when a charge is distributed evenly throughout a volume
 - $\rho \equiv Q / V$ with units C/m³
- Surface charge density: when a charge is distributed evenly over a surface area
 - $\sigma \equiv Q / A$ with units C/m²
- Linear charge density: when a charge is distributed along a line
 - $\lambda \equiv Q / \ell$ with units C/m

Amount of Charge in a Small Volume



- If the charge is nonuniformly distributed over a volume, surface, or line, the amount of charge, dq, is given by
 - For the volume: $dq = \rho \ dV$
 - For the surface: $dq = \sigma dA$
 - For the length element: $dq = \lambda d\ell$

Problem-Solving Strategy



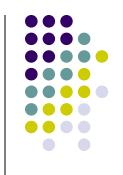
- Conceptualize
 - Establish a mental representation of the problem
 - Image the electric field produced by the charges or charge distribution
- Categorize
 - Individual charge?
 - Group of individual charges?
 - Continuous distribution of charges?

Problem-Solving Strategy, cont



- Analyze
 - Units: when using the Coulomb constant, k_e, the charges must be in C and the distances in m
 - Analyzing a group of individual charges:
 - Use the superposition principle, find the fields due to the individual charges at the point of interest and then add them as vectors to find the resultant field
 - Be careful with the manipulation of vector quantities
 - Analyzing a continuous charge distribution:
 - The vector sums for evaluating the total electric field at some point must be replaced with vector integrals
 - Divide the charge distribution into infinitesimal pieces, calculate the vector sum by integrating over the entire charge distribution

Problem Solving Hints, final



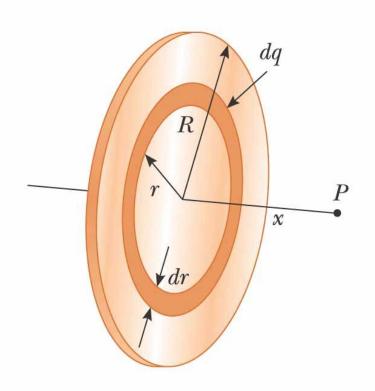
- Analyze, cont.
 - Symmetry:
 - Take advantage of any symmetry to simplify calculations

Finalize

- Check to see if the electric field expression is consistent with your mental representation
- Check to see if the solution reflects any symmetry present
- Image varying parameters to see if the mathematical result changes in a reasonable way

Example – Charged Disk

- The ring has a radius R and a uniform charge density σ
- Choose dq as a ring of radius r
- The ring has a surface area 2πr dr



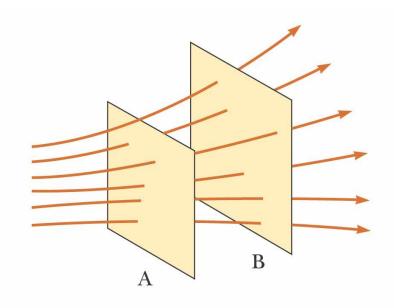
Electric Field Lines



- Field lines give us a means of representing the electric field pictorially
- The electric field vector **E** is tangent to the electric field line at each point
 - The line has a direction that is the same as that of the electric field vector
- The number of lines per unit area through a surface perpendicular to the lines is proportional to the magnitude of the electric field in that region

Electric Field Lines, General

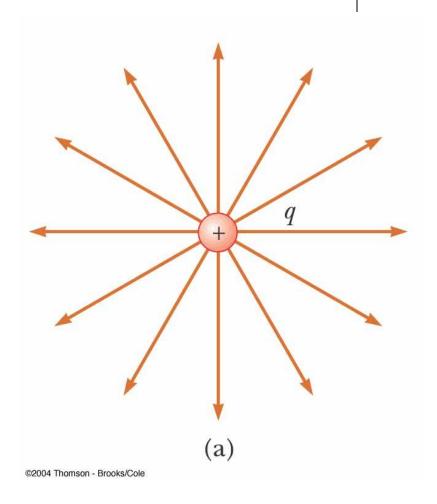
- The density of lines through surface A is greater than through surface B
- The magnitude of the electric field is greater on surface A than B
- The lines at different locations point in different directions
 - This indicates the field is nonuniform



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Electric Field Lines, Positive Point Charge

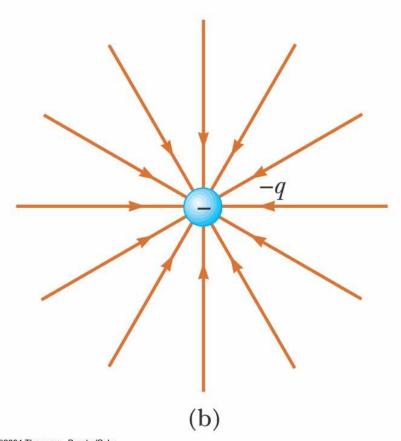
- The field lines radiate outward in all directions
 - In three dimensions, the distribution is spherical
- The lines are directed away from the source charge
 - A positive test charge would be repelled away from the positive source charge



Electric Field Lines, Negative Point Charge



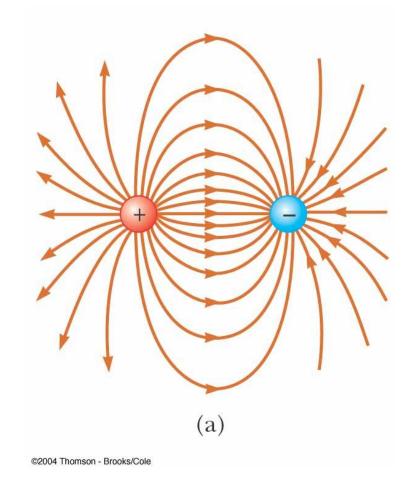
- The field lines radiate inward in all directions
- The lines are directed toward the source charge
 - A positive test charge would be attracted toward the negative source charge



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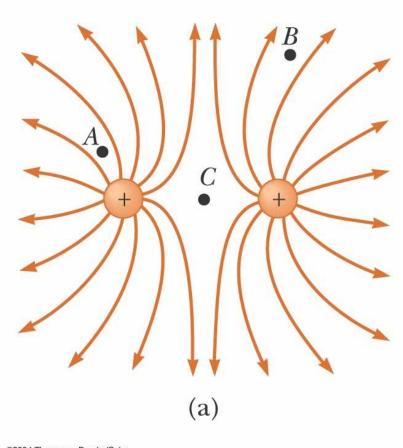
Electric Field Lines – Dipole

- The charges are equal and opposite
- The number of field lines leaving the positive charge equals the number of lines terminating on the negative charge



Electric Field Lines – Like Charges

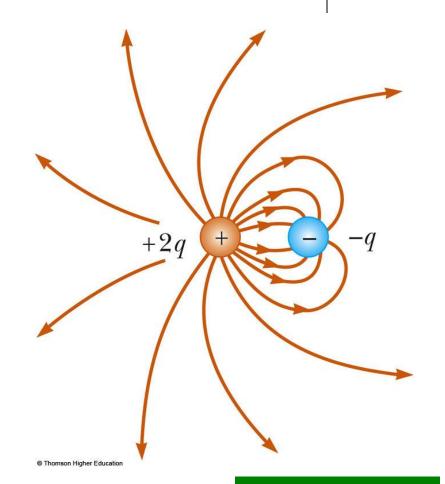
- The charges are equal and positive
- The same number of lines leave each charge since they are equal in magnitude
- At a great distance, the field is approximately equal to that of a single charge of 2q



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Electric Field Lines, Unequal Charges

- The positive charge is twice the magnitude of the negative charge
- Two lines leave the positive charge for each line that terminates on the negative charge
- At a great distance, the field would be approximately the same as that due to a single charge of +q
- Use the active figure to vary the charges and positions and observe the resulting electric field



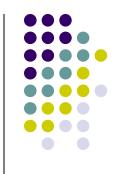
PLAY ACTIVE FIGURE

Electric Field Lines – Rules for Drawing



- The lines must begin on a positive charge and terminate on a negative charge
 - In the case of an excess of one type of charge, some lines will begin or end infinitely far away
- The number of lines drawn leaving a positive charge or approaching a negative charge is proportional to the magnitude of the charge
- No two field lines can cross
- Remember field lines are not material objects, they are a pictorial representation used to qualitatively describe the electric field

Motion of Charged Particles



- When a charged particle is placed in an electric field, it experiences an electrical force
- If this is the only force on the particle, it must be the net force
- The net force will cause the particle to accelerate according to Newton's second law

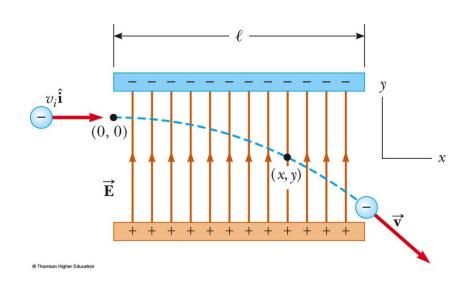
Motion of Particles, cont



- $\vec{\mathbf{F}}_e = q\vec{\mathbf{E}} = m\vec{\mathbf{a}}$
- If E is uniform, then the acceleration is constant
- If the particle has a positive charge, its acceleration is in the direction of the field
- If the particle has a negative charge, its acceleration is in the direction opposite the electric field
- Since the acceleration is constant, the kinematic equations can be used

Electron in a Uniform Field, Example

- The electron is projected horizontally into a uniform electric field
- The electron undergoes a downward acceleration
 - It is negative, so the acceleration is opposite the direction of the field
- Its motion is parabolic while between the plates



Use the active figure to vary the field and the characteristics of the particle.

PLAY ACTIVE FIGURE