

HOMEWORK – 1 (HINTS).

Chapter-24.

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4. A solid nonconducting sphere (radius = 12 cm) has a charge of uniform density (30 nC/m^3) distributed throughout its volume. Determine the magnitude of the electric field 15 cm from the center of the sphere.
- a. 22 N/C
 - b. 49 N/C
 - c. 31 N/C
 - d. 87 N/C
 - e. 26 N/C

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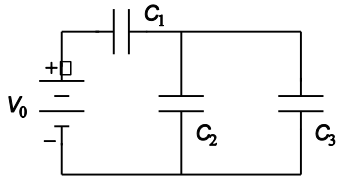
Strategy:

First, calculate the total charge of the sphere: $q = \sigma \times (\text{Volume of the sphere-R=12cm})$. The field E will be the same if the total charge is concentrated in the center of the sphere.

Use the Gauss Law: $E \times (\text{Area-of-sphere-radius-R=15 cm}) = q / \epsilon_0$.

Finally, solve for E.

7. Determine the energy stored in C_2 when $C_1 = 15 \mu\text{F}$, $C_2 = 10 \mu\text{F}$, $C_3 = 20 \mu\text{F}$, and $V_0 = 18 \text{ V}$.



- a. 0.72 mJ
- b. 0.32 mJ
- c. 0.50 mJ
- d. 0.18 mJ
- e. 1.60 mJ

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HINTS:

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Strategy:

Determine the total charge on each plate for two fragments (C_1) and (C_{23} = made of C_2 and C_3 connected in parallel). Determine the total capacitance C_{tot} of C_1 and C_{23} fragments connected in series. The total charge Q can be determined from $C_{\text{tot}} = Q / V_0$.

Q is the charge on C_1 and $Q = Q_2 + Q_3$ (Q_2 =charge on C_2 and Q_3 = charge on C_3).

We also know that: $V_0 = V_1 + V_{23}$, (V_{23} = the potential difference across C_2 or C_3), V_1 = the potential difference across C_1 .

Determine V_1 from Q and C_1 , and then V_{23} .

Finally, solve for the potential energy stored in C_2 capacitor: $U_2 = 1/2 C_2 V_{23}^2$.

8. A $30\text{-}\mu\text{F}$ capacitor is charged to an unknown potential V_0 and then connected across an initially uncharged $10\text{-}\mu\text{F}$ capacitor. If the final potential difference across the $10\text{-}\mu\text{F}$ capacitor is 20 V , determine V_0 .

- a. 13 V
- b. 27 V
- c. 20 V
- d. 29 V
- e. 60 V

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HINTS:

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Strategy:

Use the conservation law of the total electric charge.

Before the connection (initial-situation):

$$Q(\text{initial}) = C_1 \times V_0 ,$$

(Here, $C_1 = 30\text{-}\mu\text{F}$)

After the connection: $Q(\text{final}) = C_1 \times V_f + C_2 \times V_f.$

(Here, $C_1 = 30\text{-}\mu\text{F}$, $C_2 = 10\text{-}\mu\text{F}$, $V_f = 20\text{ V}$)

Charges must be preserved: $Q(\text{initial}) = Q(\text{final}).$

Finally, solve for V_0 .